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LECTURE 06: WEIGHTED AVERAGE

I. Mean, Median, Mode Practice
    a. [This video](#) covers mean, median, mode, and standard deviation.
    b. Excel has the equations for mean, median, and mode built into it.
        i.   For mean, type "=AVERAGE" and press the TAB key. Then highlight the cells you wish to find the average of and press ENTER.
        ii. For median, type "=MEDIAN" and press the TAB key. Then highlight the cells you wish to find the median of and press ENTER.
        iii. For mode, type "=MODE" and press the TAB key. Then highlight the cells you wish to find the mode of and press ENTER.
    c. Open Data Set 2 which contains historic data on Disney's total sales and sales by division. (Under Disney Sales sheet.)
    d. Which division has the most revenue growth for a particular year? That's indicated in Column B and to answer that question we need to find the mode.
        i. The mode is a mathematical operation so Excel needs to analyze numbers. I assigned each division a number and indicated the appropriate number in Column C.
        ii. In A22, type "Mode" and then type "=MODE(C5:C21)" in C22. You should get 3, or Parks and Resorts.
    e. In A23, type "Mean" and find the average sales of the five different divisions plus the total sales average.
        i. For example, in D23 type "=AVERAGE(D4:D21)"
        ii. Note once typed, you can select and copy the cell and then paste it in the appropriate places; the references will update automatically.
    f. In A24, type "Median" and find the median sales of the division plus the total.
        i. For example, in D24 type "=MEDIAN(D4:D21)"
II. Weighted Average
    a. Sometimes some observations matter more than others and you want to give more emphasis to those when finding an average.

b. That additional emphasis is called a "weight." Using a normal average, all observations have equal weight. With a weighted average, each observation has a weight assigned to it. That observation's value is multiplied by the weight before being added. You then divide not by the total number of observations but by the sum of the weights:

$$Weighted\ Average = \frac{\sum_i^n (w_i x_i)}{\sum_i^n w_i}$$

    i. Where x_i is the ith observation; and

    ii. w_i is the weight for that ith observation.

c. Examples:

    i. <u>Your grade</u>. Each assignment may have the same possible points but each one is weighed as indicated in the syllabus. I use the equation above to calculate your final grade.

    ii. <u>Stock markets</u>. Some stock market indicators, like the S&P 500, weigh the price of each company's stock by how many stocks of that company exist.

    iii. <u>Slugging average</u>. This baseball statistic measures how many bases a single player gets to when the batter hits the ball. The number of times a player can pass three bases has more weight than the number of times a player can make it to only one base.

d. Typically weights are less than one and the sum of all weights equal one (thus dividing is not necessary because you'll just be dividing by one). But not always.

    i. Sometimes while the weights equal one, not all the information is there and you end up dividing by the sum of all the weights for the information you have. I do this when a student wants to know his/her current grade before every assignment is complete.

    ii. Other times the weights are quantities. The example from II was technically a weighted average. I multiplied each value by the weight and then divided the whole thing by the sum of the weights.

e. Consider a harder example: MPG. Here's a table of hypothetical data concerning gas mileage.

MPG	Miles	Gallons
100	50	0.5
50	400	8.0

    i. What's the average MPG? It would be a mistake to claim it's 75—the simple average between the two observations—because one observation has many more miles and gallons to it. That observation should have greater weight.

    ii. What we can do is add a percent value to each observation, multiply the MPG by the percent, and then sum the products to find the weighted average. The question is, should the percent be based on miles or on gallons?

    iii. Since MPG is based on miles *per gallon* (in other words, gallons are in the denominator), we base the percent on gallons. About 94.1% (8/8.5) of miles drove was as 50 MPG. About 5.9% (0.5/8.5) of miles drove was as 100 MPG. 0.941*50 + 0.059*100 = 52.9.

    iv. Note that if we add up all the miles (450) and divide by all of the gallons (8.5), we get also 52.9. Nice way to check the work.

III. Weighted Average Practice

    a. In the next sheet, under Performance Review, there is a hypothetical Disney employee named Andy. Suppose Disney determines if people get a raise based on three criteria: how often they take sick days (Attendance), what customers say about them (Customer Reviews), and their sales (Sales).

    b. Each criterion has weights, as indicated, and Andy gets the scores as indicated. Each is out of 100.

        i. Andy is a great salesperson but he's also very rude to a few people; he has a fair number of complaints.

    c. Suppose Disney requires a score of 85 to qualify for a raise. To determine if Andy gets it:

        ii. In D3, type "=B3*C3". Note we are multiplying the weight by the score.

        iii. Copy this cell in D4 and D5.

        iv. In D6, type "=SUM(D3:D5)". You should get a result of 87. Andy (barely) gets his raise.

        v. You can also use the "=SUMPRODUCT" function to sum the products of two columns ("arrays").

d. You can also divide the result in D6 by the sum of all the weights. This isn't important here as the sum of the weights equal 1, but it's what you do when they don't equal 1.
   a. Imagine, for example, that Andy didn't know the reviews said but he did know the other criteria. In that case, he would multiple 0.10 times 90 and add that to 0.60 times 100. Then he would divide the result—69—by 0.7 to get 98.6.